

# On Simultaneous Lyapunov Diagonal Stability

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## **Abstract**

The problem of simultaneous Lyapunov diagonal stability (viz. the existence of a common diagonal Lyapunov solution for systems of Lyapunov matrix inequalities) on a matrix set  $\mathcal{A}$  arises from the study of Lyapunov diagonal stability on a single matrix and from the area of interconnected time-varying and switched systems. In this talk, we present two characterizations for simultaneous Lyapunov diagonal stability, one through a theorem of the alternative for linear maps on inner product spaces and the other through Hadamard products of the matrices in  $\mathcal{A}$  and a new notion called  $\mathcal{P}$ -sets. Applications of these results are also provided.