MH 1710, Final Exam .

NAME_

SHOW ALL WORK

1. (3 pts each) (a) Sketch $\vec{B} - \vec{A}$. (b) Sketch $\vec{B} + \vec{A}$.

(c) Sketch the projection of \vec{B} onto \vec{A} .







- 2. Let $\vec{A} = (1, 1, 2), \ \vec{B} = (-1, 1, 1), \ \text{and} \ \vec{C} = (1, 2, 3).$
 - (a) Find the cosine of the angle between \vec{A} and \vec{B} .
 - (b) Find the projection of \vec{A} onto \vec{B} .
 - (c) Find a unit vector that points in the direction of \vec{A}
 - (d) Find $\vec{A} \times \vec{B}$.
 - (e) Find a vector that is perpendicular to both \vec{A} and \vec{B} .
 - (f) Find the volume of the parallelopiped with adjacent edges \vec{A} , \vec{B} , and \vec{C} .
 - (g) Find the area of the triangle with verticies \vec{A} , \vec{B} , and \vec{C} .
- 3. The graph of a function f is sketched below.



- (a) Determine the segments where f' > 0
- (b) Determine the segments where f' < 0
- (c) Determine where the graph of f has a horizontal tangent line.
- (d) Where does f' fail to be defined?
- (e) Where does f fail to be continuous?
- 4. The graph of the **DERIVATIVE** of f is sketched below.



- (a) Determine where f attains its maximum.
- (b) Determine where f is concave up.
- 5. (10 pts each) Find the derivative of:
 - (a) $f(x) = (4x^{-3/2} + 2x^2 x^{-2} + \pi)(x^{-3} x^{4/7} + 3).$
 - (b) $f(x) = (\sin(6\pi x) + 4)/(\cos(5x + 2)).$
 - (c) $f(x) = \tan(3x) + \sec(5x+1) + \cot(x)$.
 - (d) $f(x) = e^{(x^2)} + \ln(x^3 + 2)$
- 6. (10 pts) Find an equation for the line tangent to $f(x) = (x^{-3} + x^2 + 1)$ at $x_0 = 1$.
- 7. (10 pts) Parameterize the line tangent to $\vec{r}(x) = (\cos(3\pi x), \sin(\pi x), \ln(2x))$ at $x_0 = 1/2$.
- 8. (10 pts) One leg of a right triangle is fixed at 3 meters as the other leg is decreasing at a rate of 2 m/sec. What is the rate of change of the area of the triangle when the leg of variable length is 1 meter long?
- 9. (15 pts) Let $f(x) = \frac{x^3}{3} + 3x^2 + x$.
 - (a) Determine where f is increasing and where f is decreasing.
 - (b) Determine the concavity of f.
 - (c) Sketch.
- 10. (10 pts) Find the maximum value for $f(x) = \sin(x)\cos(x)$ on the interval $0 \le x \le 2\pi$.
- 11. (5 pts each) $\vec{r}(t) = (x(t), y(t))$. You are given the graphs of x(t) and y(t) below.



- (a) Determine where the curve parametrized by \vec{r} has a horizontal tangent line.
- (b) Determine where the curve parametrized by \vec{r} has a vertical tangent line.

12. (10 pts each) Let
$$F(x) = \int_2^x \frac{t \, dt}{(t+5)(t-4)}$$

- (a) Determine the domain of F.
- (b) Find the derivative of F.
- 13. (10 pts each) Evaluate

(a)
$$\int x^2 (x^3 + 1)^{99} dx.$$

(b)
$$\int \frac{x^2}{x^3 + 1} dx.$$

(c) $\int x^2 e^{x^3 + 1} dx.$
(d) $\int_0^1 \frac{d}{dx} (x^3 + 6x^2)^{2x} dx.$
(e) $\int_0^{\pi/2} \sin^3 x \cos x \, dx.$