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C L Frota^{*} (clfrota@uem.br), Universidade Estadual de Maringá, Departamento de Matemática, AV. Colombo, 5790, Maringá, Paraná 87020-900, Brazil, and H R Clark, J Limaco and A T Cousin. On dissipative Boussinesq equation in a non-cylindrical domain.

We consider the initial-boundary value problem for the one-dimensional in space dissipative Boussinesq equation in a noncylindrical domain of \mathbb{R}^2 , namely

$$u_{tt}(x,t) - \left(u(x,t) + u_t(x,t) + u^2(x,t)\right)_{xx} + u_{xxxx}(x,t) = 0 \quad \text{in} \quad \widehat{\mathcal{Q}},$$
(1)

$$u(\alpha(t), t) = u(\beta(t), t) = u_x(\alpha(t), t) = u_x(\beta(t), t) = 0 \quad \text{for} \quad t \ge 0,$$
(2)

$$u(x,0) = u_0(x); \ u_t(x,0) = u_1(x) \quad \text{for} \quad x \in [\alpha_0,\beta_0].$$
 (3)

Here α and β are real functions defined on $[0,\infty)$, $\alpha(0) = \alpha_0 < \beta_0 = \beta(0)$ and

$$\widehat{\mathcal{Q}} = \left\{ (x,t) \in \mathbb{R}^2 : \ \alpha(t) < x < \beta(t) \quad \text{and} \quad t \ge 0 \right\}$$

is a noncylindrical domain. The noncylindrical domain \widehat{Q} means that the beam at rest is model by the interval $[\alpha_0, \beta_0]$ and its ends change in time according the functions $\alpha(t)$ and $\beta(t)$, due for instance by a temperature variation. We prove the global solvability to this problem and the exponential decay for the associated energy as $t \to \infty$. (Received January 22, 2008)