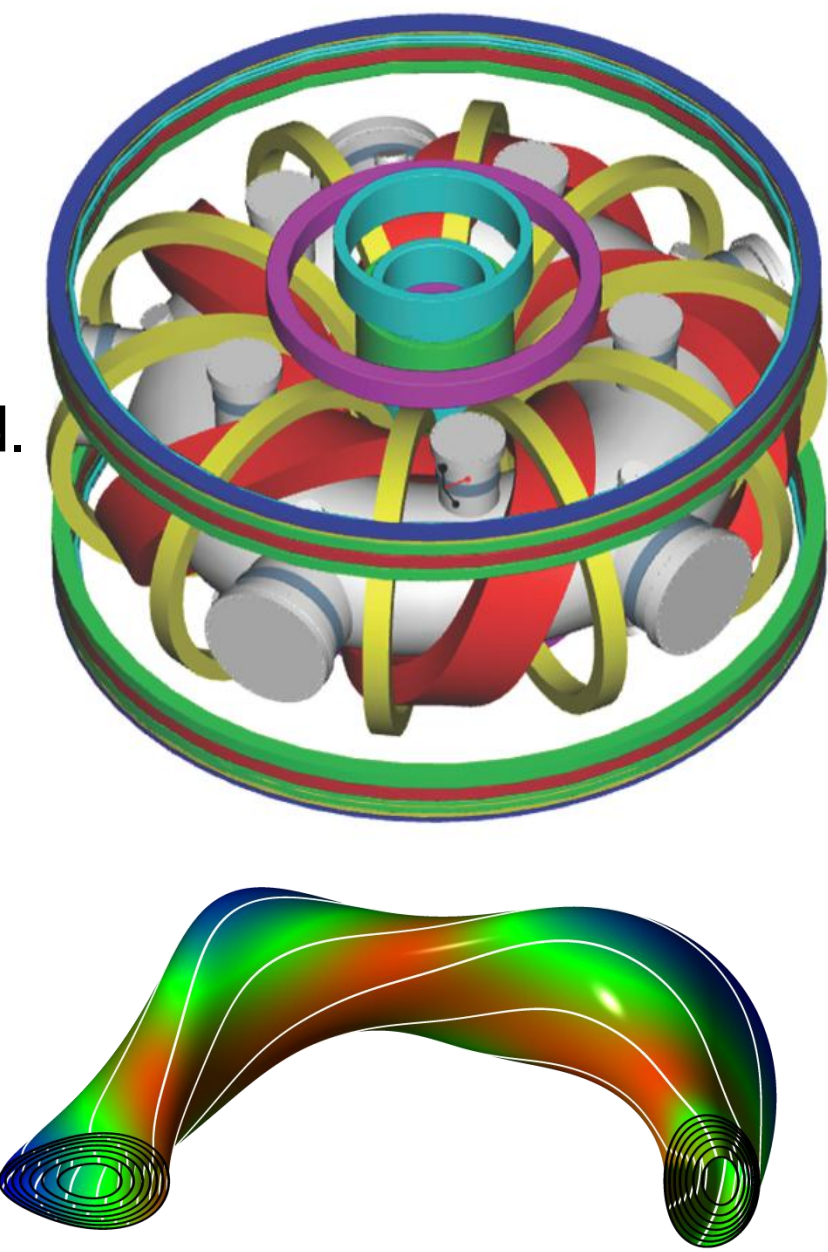


## Introduction & Motivation

- Sawteeth oscillations are tied to a 1/1 MHD mode, but other important aspects are not clearly understood.
- How do sawtooth properties depend on total and vacuum transform?
- Due to the unique nature of CTH, the vacuum and total transform can be varied.
- The size of the inversion radius and characteristics such as the rise and crash timescales are investigated as functions of the total and vacuum rotational transform.

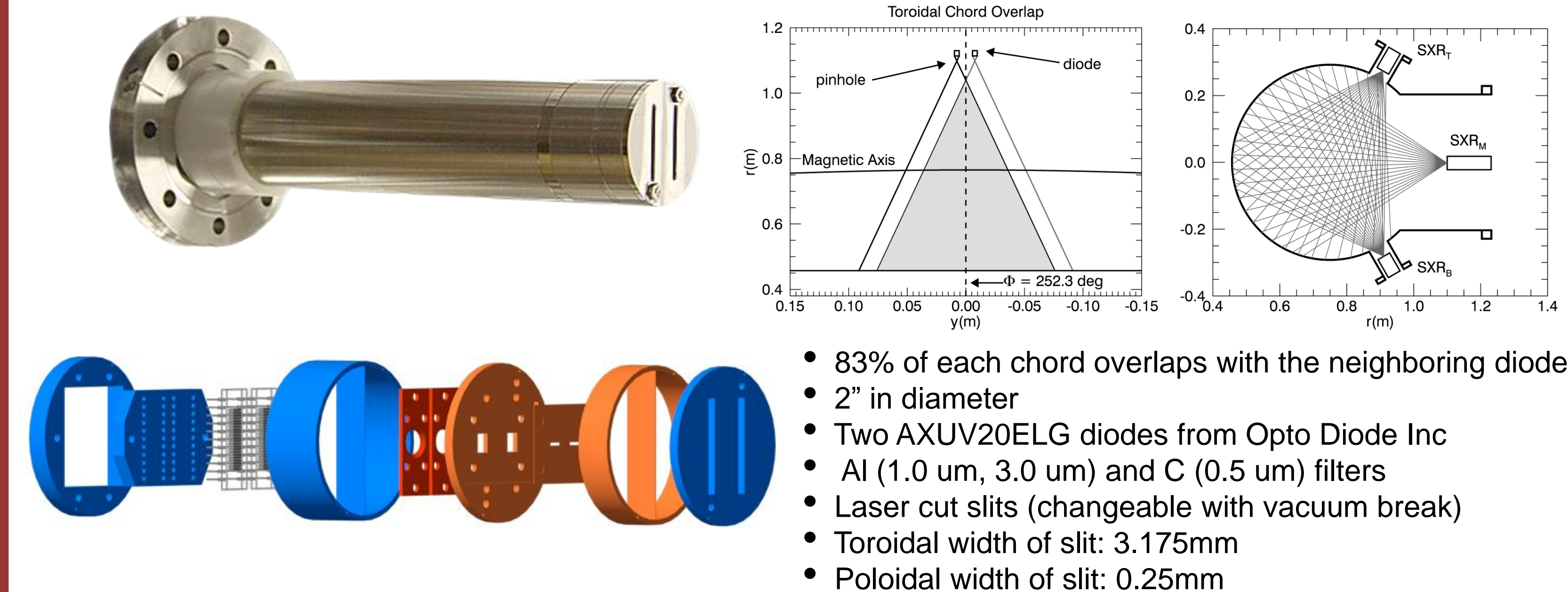


### Compact Toroidal Hybrid (CTH)

- $l=2$ , 5 field-period torsatron with auxiliary toroidal field coils
  - Operates as conventional torsatron with ECRH plasma generation
  - Toroidal plasma current driven with an OH solenoid increases density and temperature
- Parameters:
- |                   |                                    |                              |   |                                |
|-------------------|------------------------------------|------------------------------|---|--------------------------------|
| $R_0 = 0.75$ m    | $P_{\text{input}} \leq 30$ kW ECRH | $a_{\text{vessel}} = 0.29$ m | $n_e \leq 5 \times 10^{19}$ m <sup>-3</sup> | $a_{\text{plasma}} \leq 0.2$ m |
| $T_e \leq 200$ eV | $B_0 \leq 0.7$ T                   | $\beta \leq 0.5\%$           | $I_p \leq 80$ kA                            | Discharge duration – 0.1 s     |

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## Two-Color Diagnostic on CTH



## Theory of Two-Color SXR $T_e$

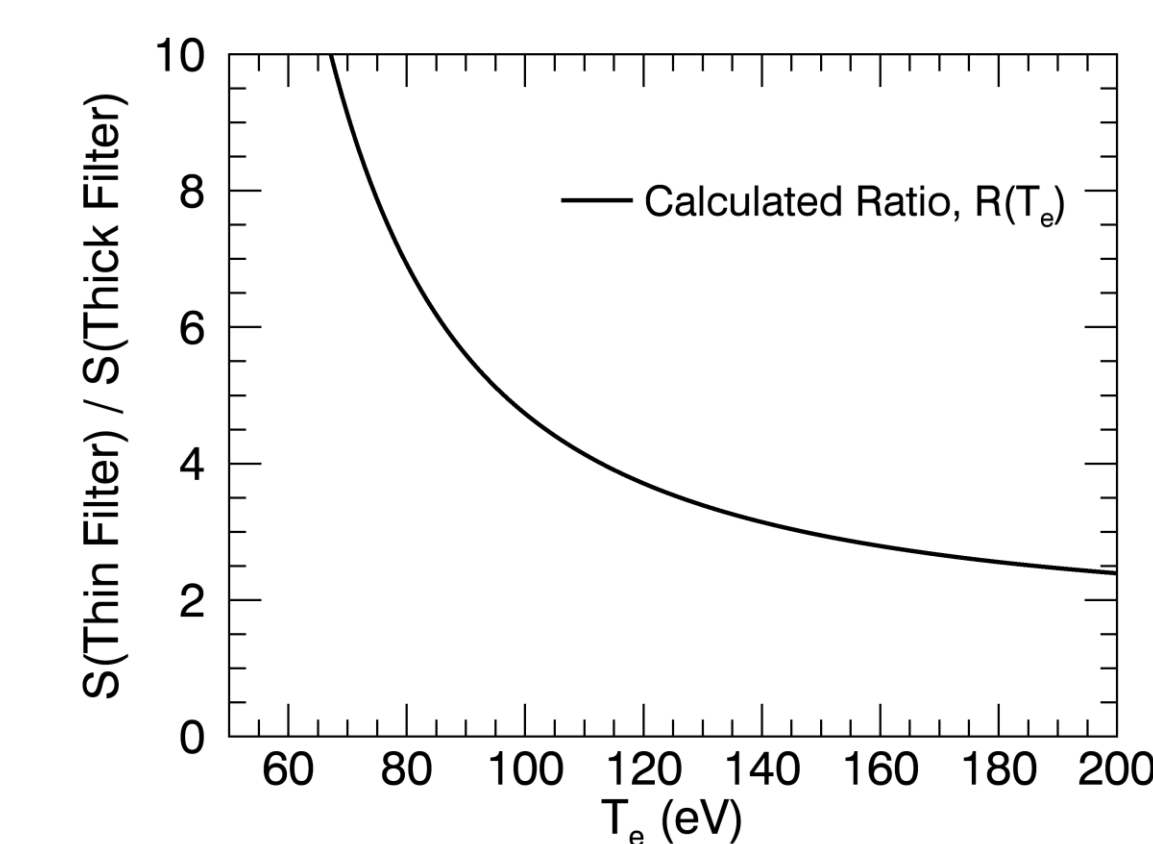
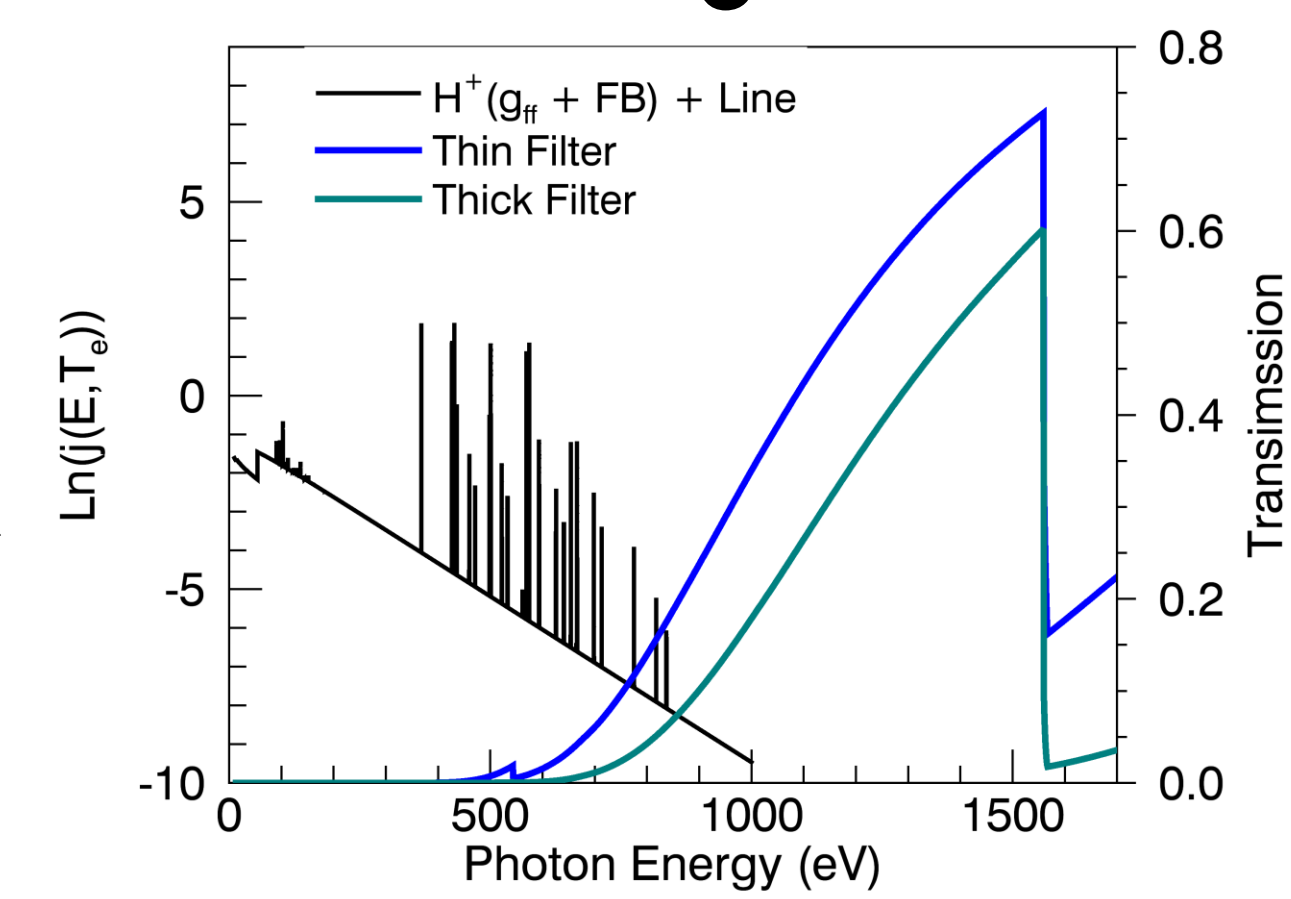
- Each filter has a different photon cut-off energy (bold lines) limiting the lower energy range of the bremsstrahlung radiation.
- The filters are 0.5  $\mu$ m C and 1.0  $\mu$ m or 3.0  $\mu$ m Al. A 0.5  $\mu$ m Al<sub>2</sub>O<sub>3</sub> layer was assumed as the dominant impurity for both filters.
- The bremsstrahlung radiation was simulated using Atomic Data and Analysis Structure (ADAS) code<sup>2</sup> at:  $n_e = 2 \times 10^{19}$  m<sup>-3</sup>,  $T_e = 100$  eV.

The SXR signal for each chord with a filter of thickness  $t_1$  is calculated using the formula:

$$SXR(t_1) = k \int_0^\infty dE \int_V j(E, T_e) A(E) T(E, t_1) \frac{d\Omega}{4\pi} dr$$

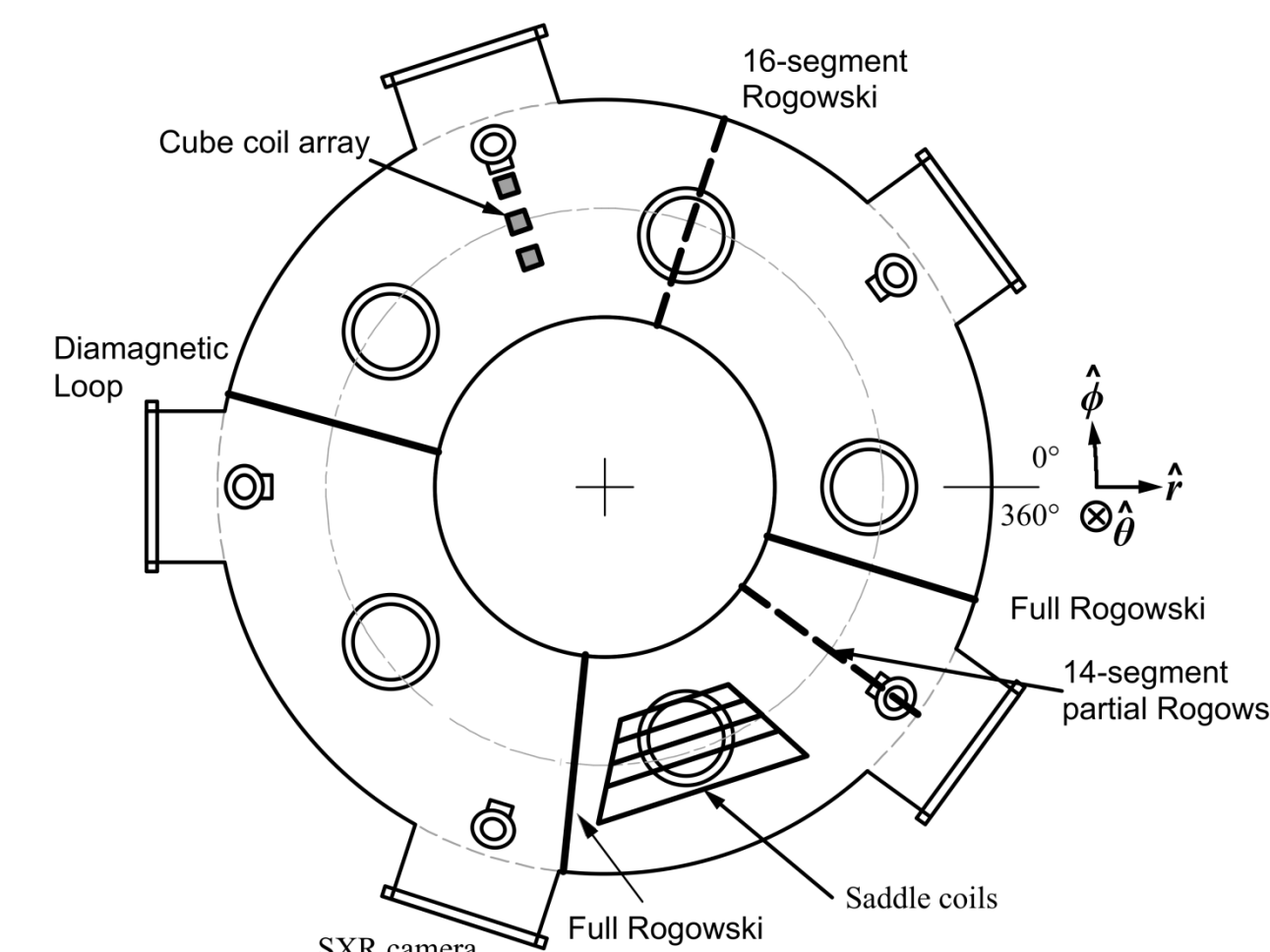
- $A(E)$  is the absorption coefficient of the photodiode,  $T$  is the transmission of the filter,  $j$  is the bremsstrahlung radiation.

- The temperature is determined by comparing the ratio of experimental signals to the theoretical ratio.

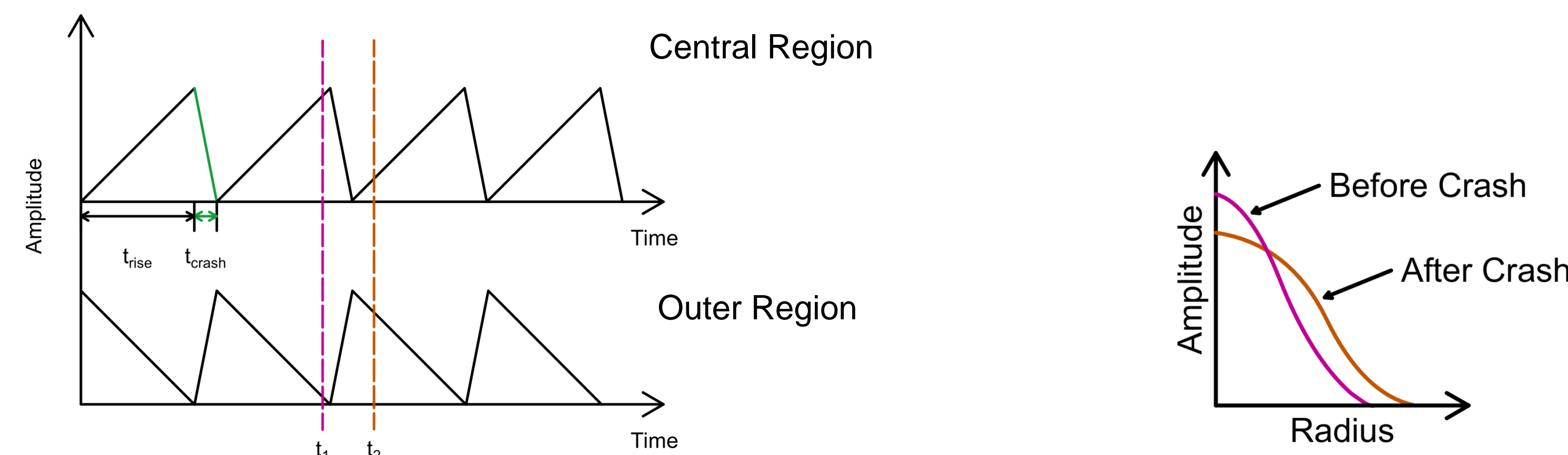


## Reconstructions using V3FIT

- V3FIT<sup>3</sup> is used to reconstruct a fully 3D plasma equilibrium.
- V3FIT finds the best fit between data signals calculated from the given equilibrium model and experimental values.
- CTH uses VMEC<sup>4</sup> as the equilibrium solver for V3FIT.
- VMEC is an ideal MHD equilibrium solver. It can calculate the 3D closed nested flux surfaces in toroidal plasmas.
- Experimental values from 186 diagnostics including: Rogowski, cube coils, saddle coils, and SXR signals are used to compute the equilibrium model.

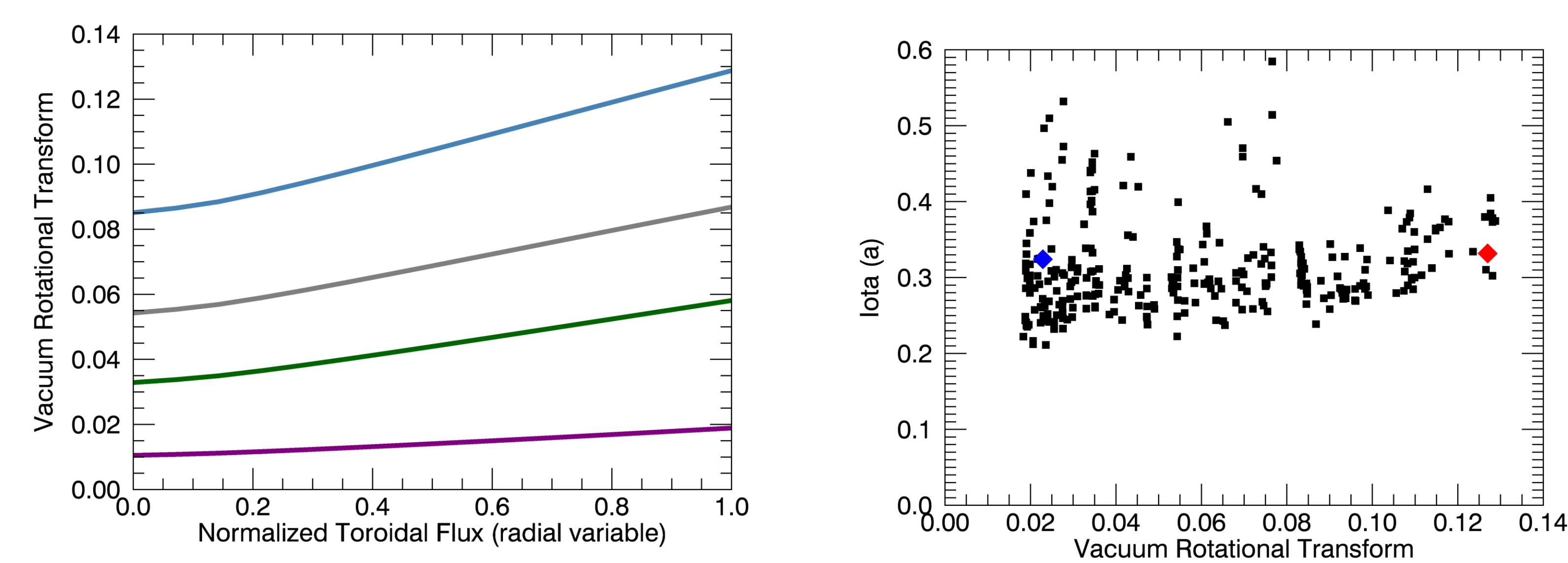


## Sawtooth Instability in CTH

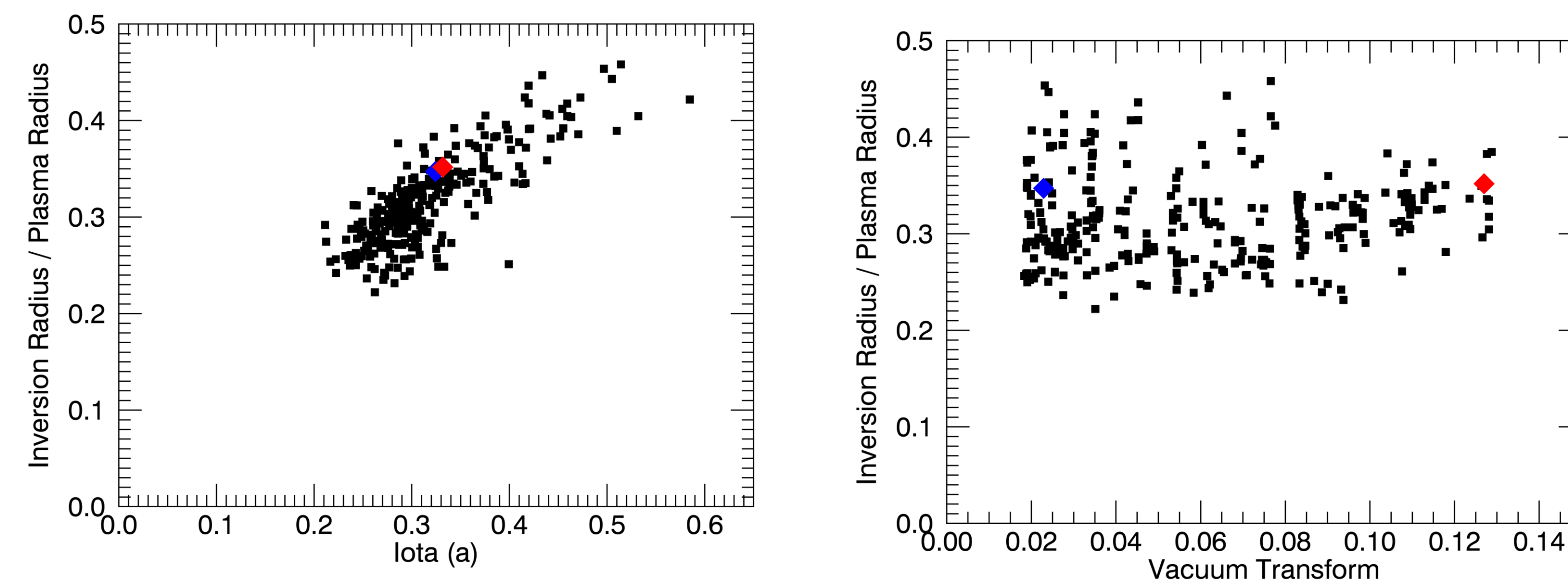


- The core of the plasma is heated ohmically, peaking the plasma current and temperature therefore letting  $q$  drop below unity.
- A  $m=1$ ,  $n=1$  MHD mode then grows until the core confinement is lost and expels the energy to the outer regions.
- Schematic of current density and electron temperature profiles
- They peak during the ramp and flatten after a crash.

### Sawtooth Scan – Changing the vacuum transform

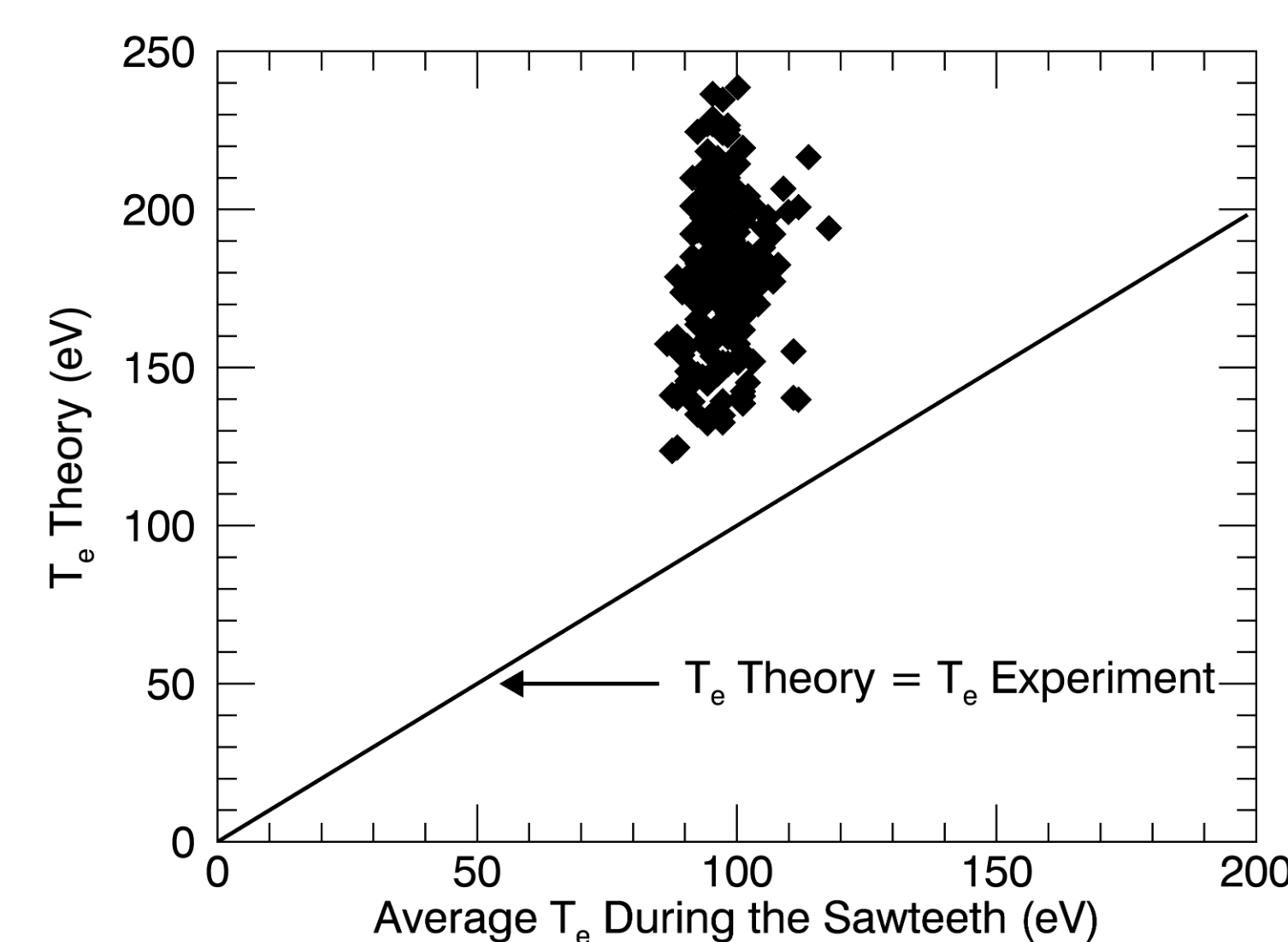


### Sawtooth inversion radius scales with total edge transform



- The inversion radius is where the iota surface is equal to 1
- Snider<sup>5</sup> found the ratio of the inversion radius to the plasma radius to increase with increasing iota.
- This phenomena is observed with the sawteeth on CTH.

### Temperature for the onset of sawteeth

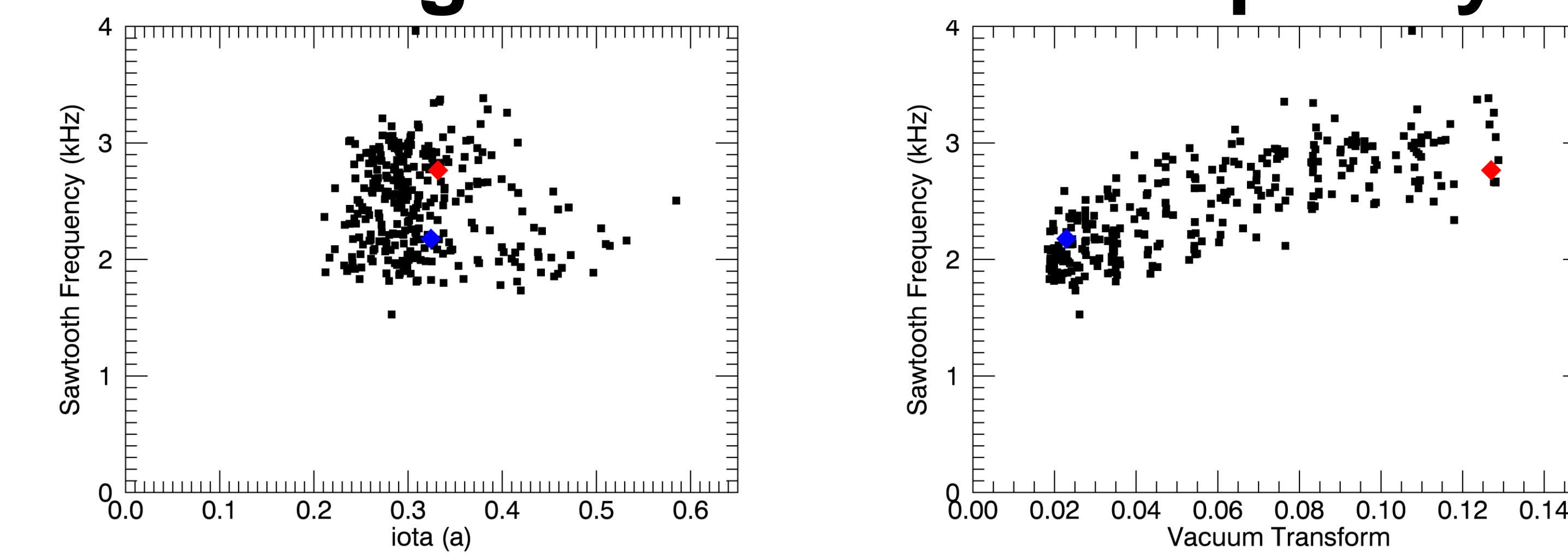


A temperature requirement for the onset of sawteeth with a  $q=1$  surface in the plasma interior is given by<sup>1</sup>:

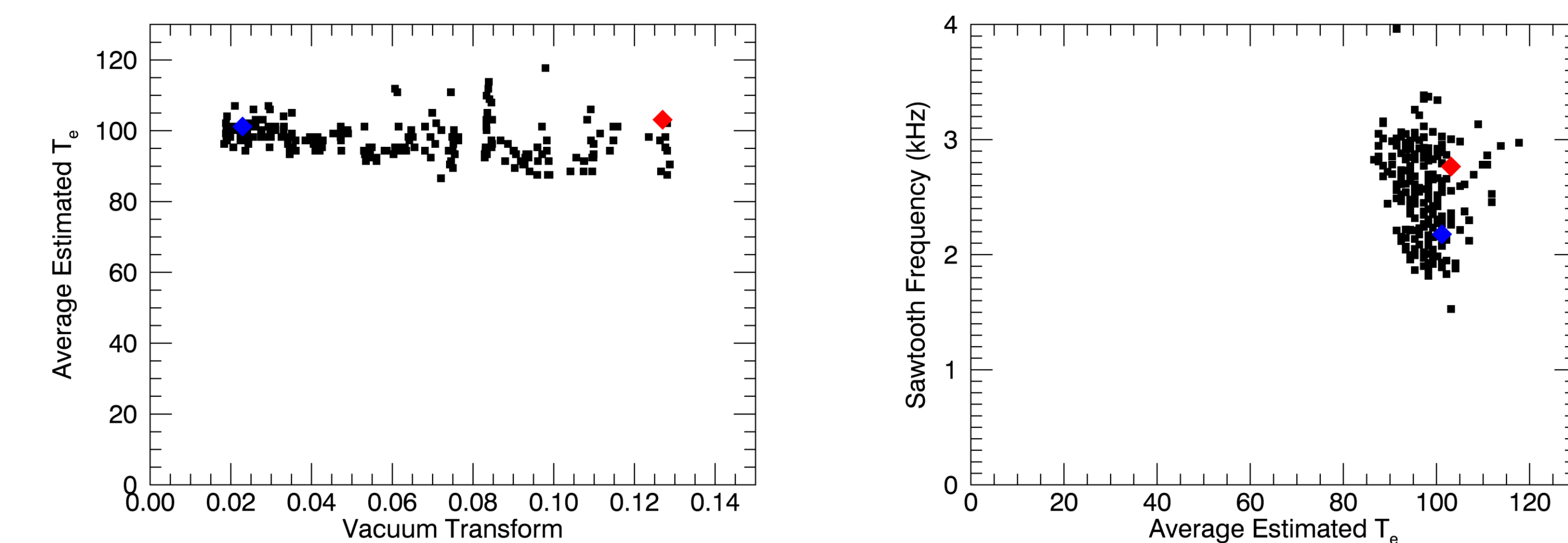
$$1 = \frac{4\pi B_z}{\mu_0 V} \eta$$

- Using  $B_z$  calculated from reconstructions,  $\ln(\Lambda) = 15$ ,  $Z_{\text{eff}} = 1.5$ , and the loop voltage from the experiment gives an estimated temperature using Spitzer resistivity.
- The loop voltage was assumed to be constant across the plasma.
- This x-axis is the average electron temperature in the core of the plasma when sawteeth are observed.

## Change in Sawtooth Frequency



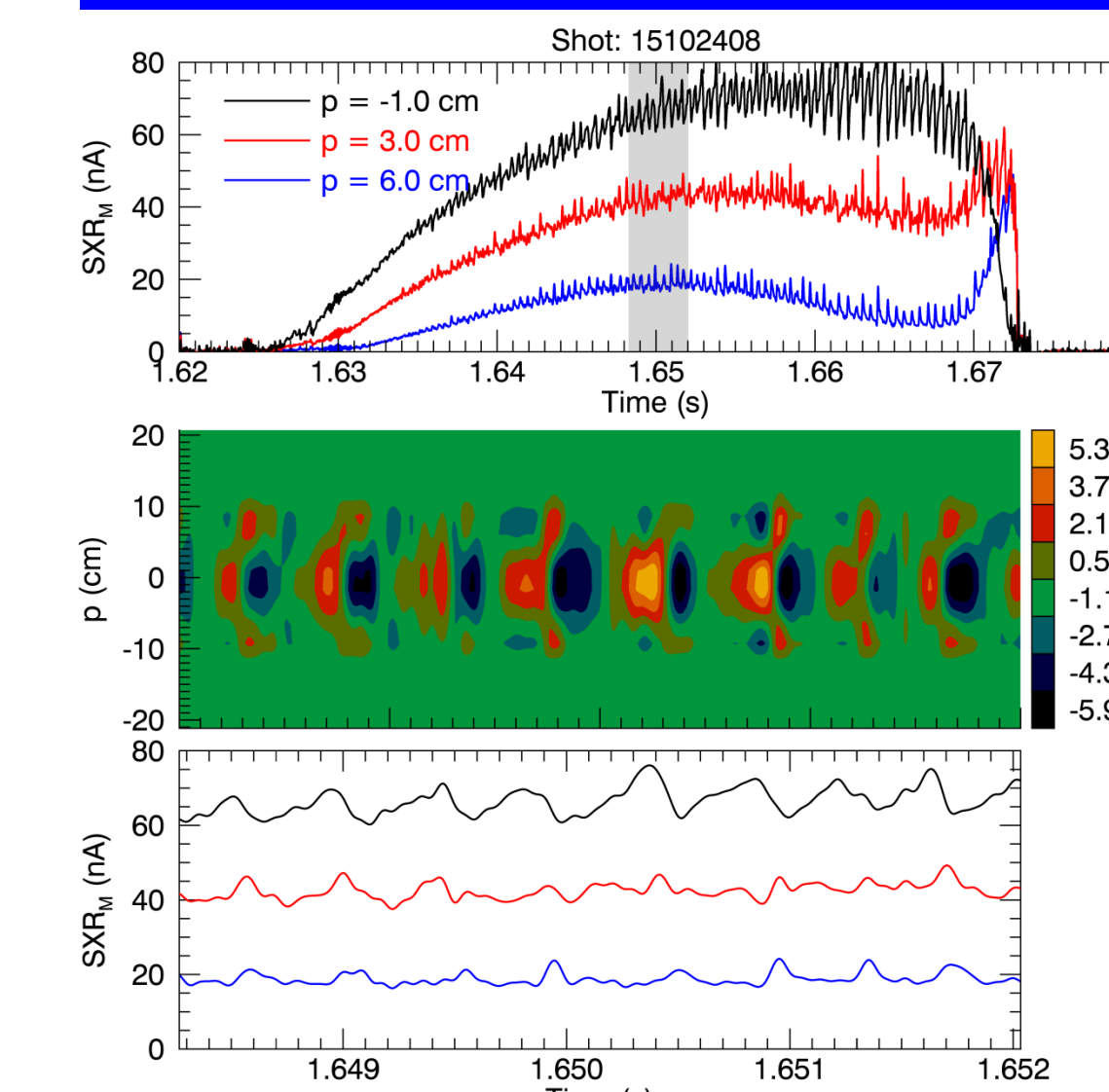
- The sawtooth frequency appears to be independent of the total edge transform during a discharge, but dependent on the vacuum transform of the stellarator equilibrium applied before the discharge.
- The sawtooth rise time increases with the vacuum transform, while the crash time does not (not shown).



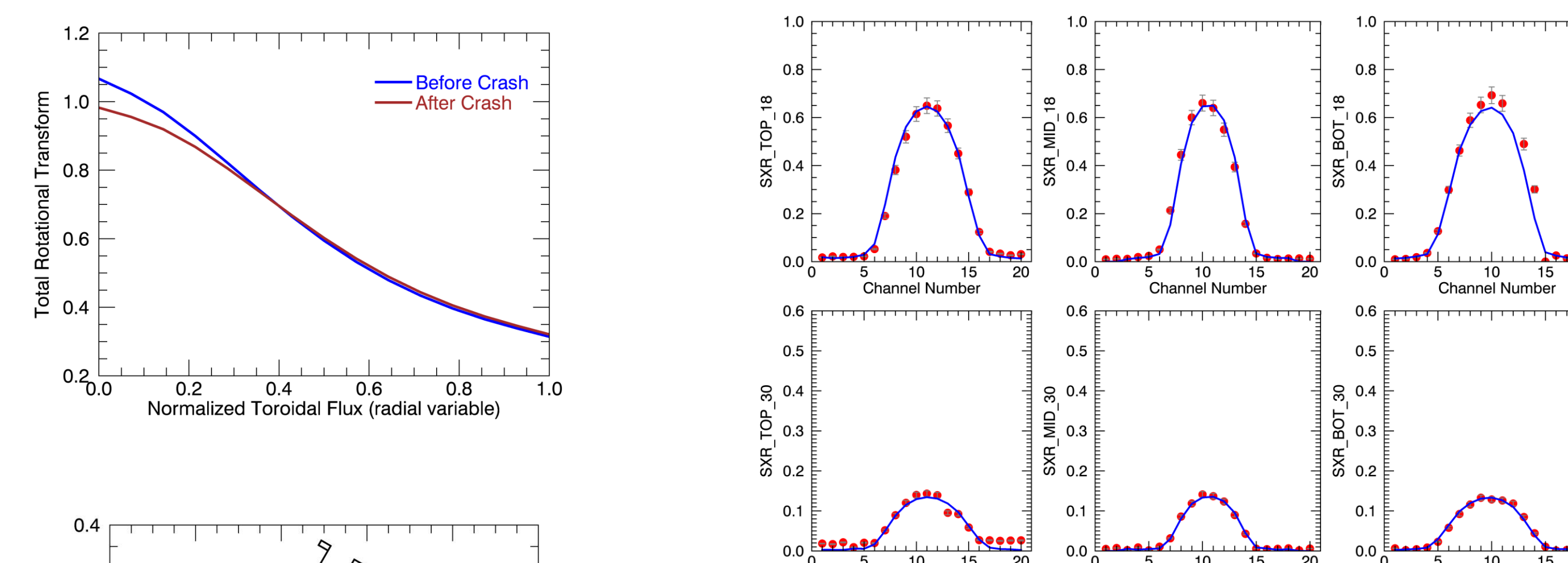
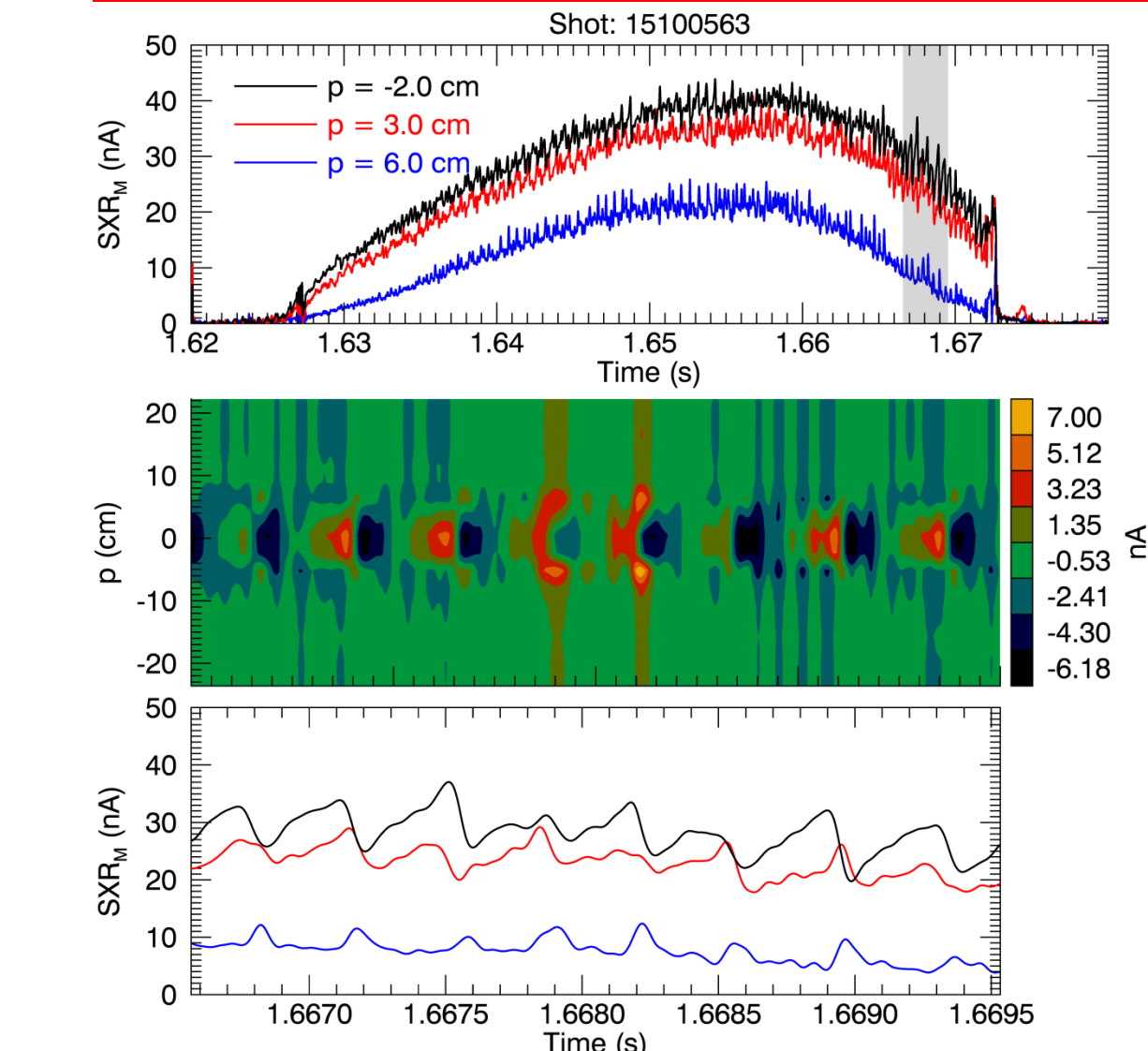
- It has been found that the sawtooth period increases as the central temperature increase on JET.<sup>6</sup>
- The sawteeth period does not seem to scale with electron temperature for CTH plasmas.
- The heating rate a sawtooth was given by Jahns<sup>1</sup>,  $Q_{ei}$  is the electron-ion energy,  $Q_r$  is the radiation loss rate.

$$\left. \frac{dT_e}{dt} \right|_{r=0} = \frac{2}{3} \frac{1}{n(0)} \left[ \eta J_z^2 - Q_{ei} - Q_r \right]_{r=0}$$

### Low vacuum transform



### High vacuum transform



- Reconstruction for the low vacuum transform case.
- The reconstructed iota = 1 surface matches up with the measured inversion radius.

## References

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